

**CENTRO INTERDIPARTIMENTALE DI RICERCA
«CENTRO STUDI DI ECONOMIA E
TECNICA DELL'ENERGIA
GIORGIO LEVI CASES»**

PRESENTAZIONE PROGETTO DI RICERCA

**A photobioreactor-on-a-chip technology
for assessing and optimising photosynthetic activity
in microalgae-based fuel production**

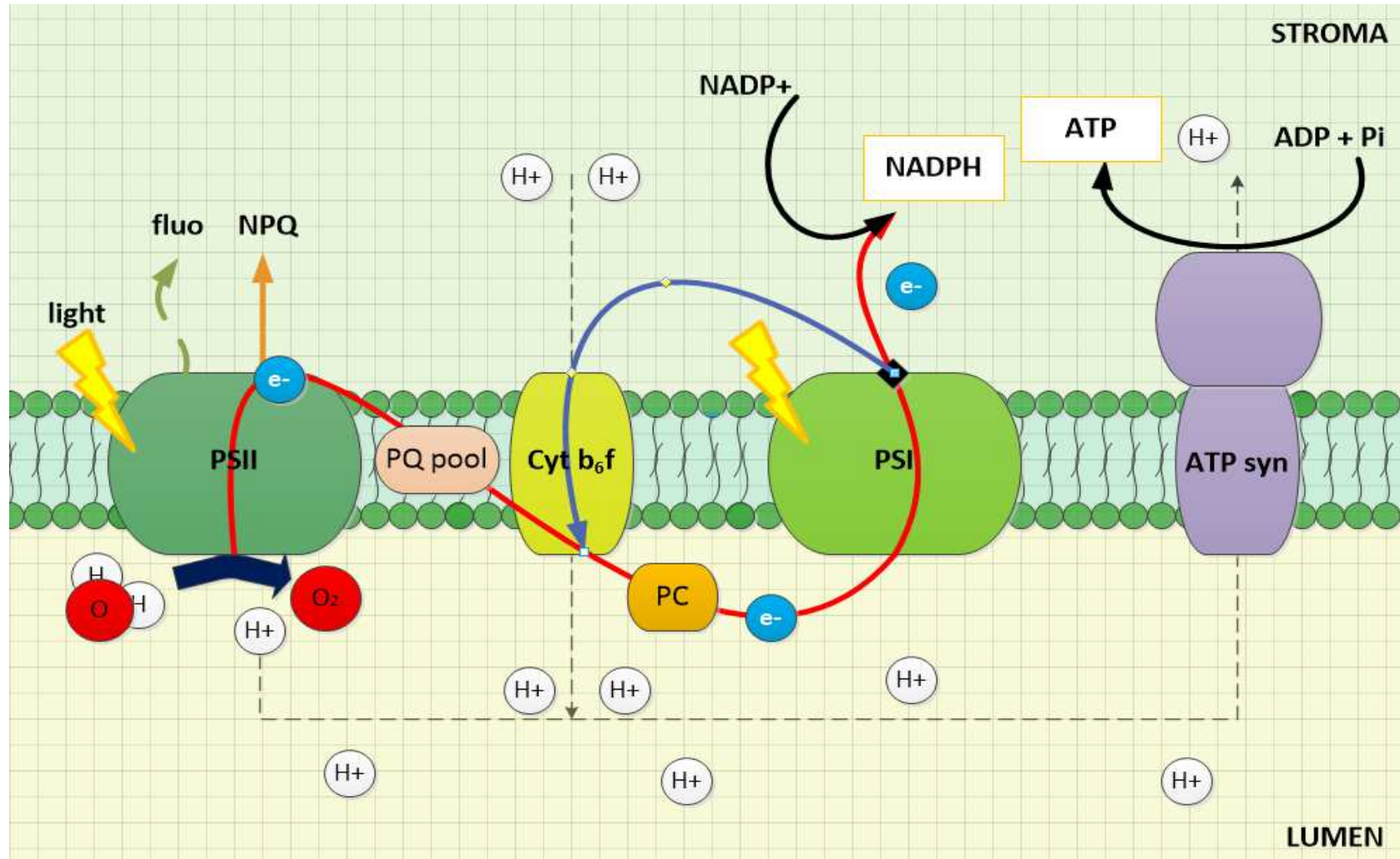
Giovedì 19 febbraio 2015

Prof. Fabrizio Bezzo

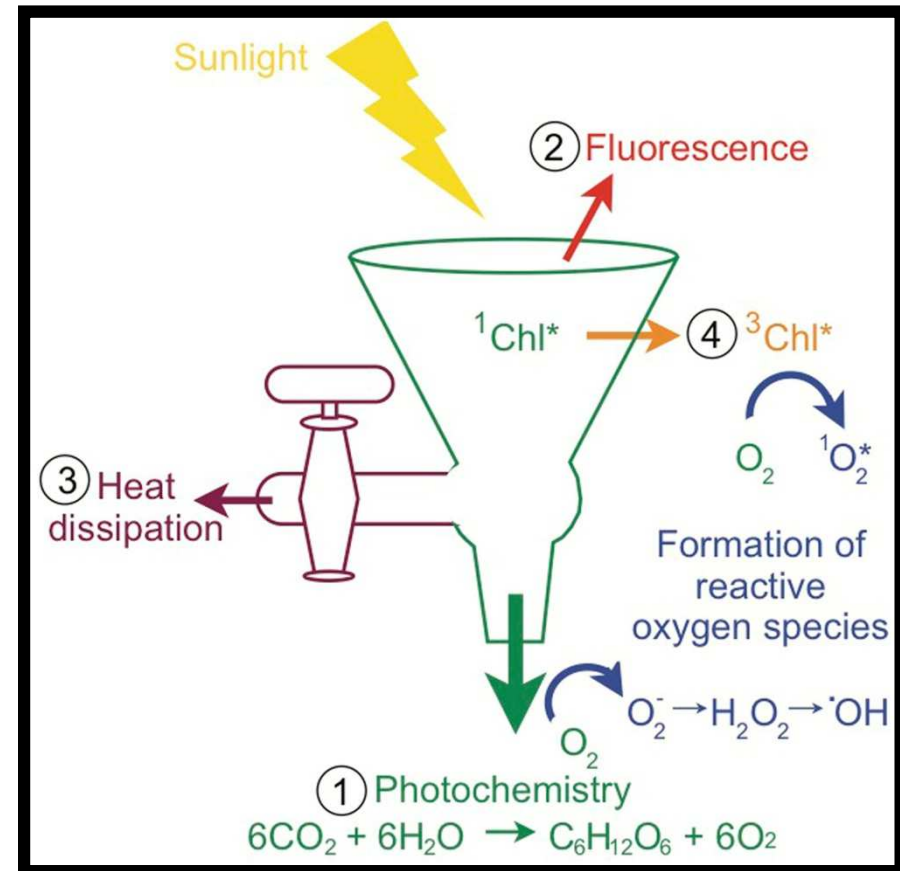
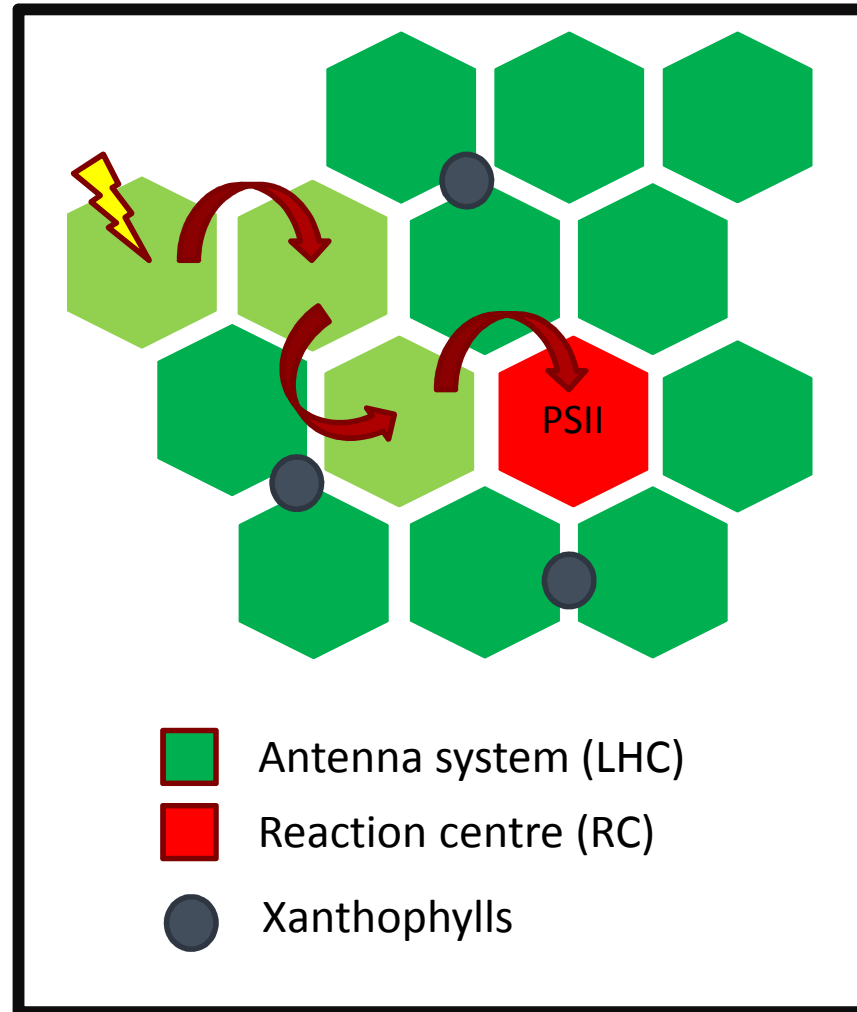
Aim of the work

- Develop reliable dynamic model photosynthetic phenomena
- Propose an effective investigation tool through microscale devices

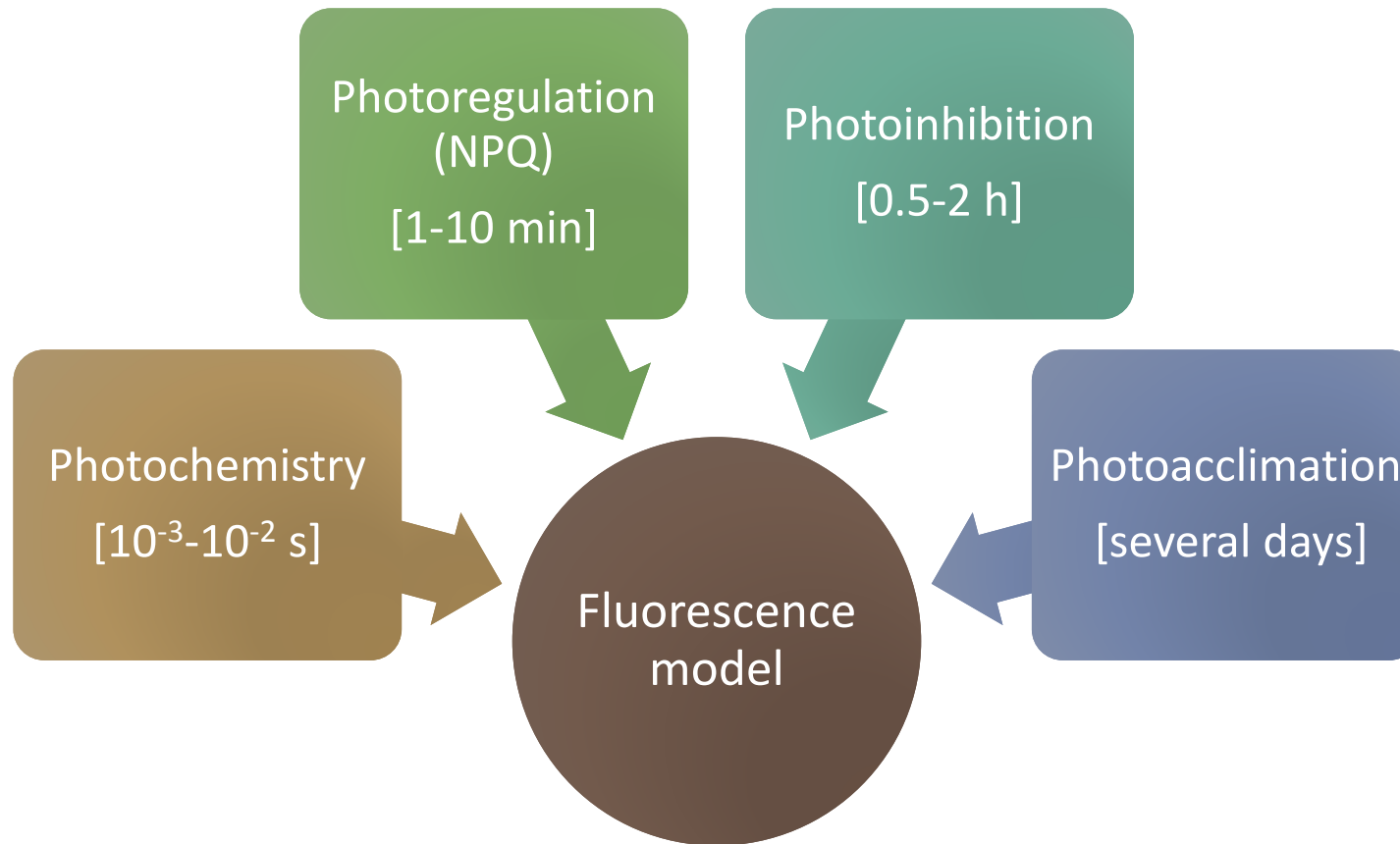
Photosynthetic process scheme (1)



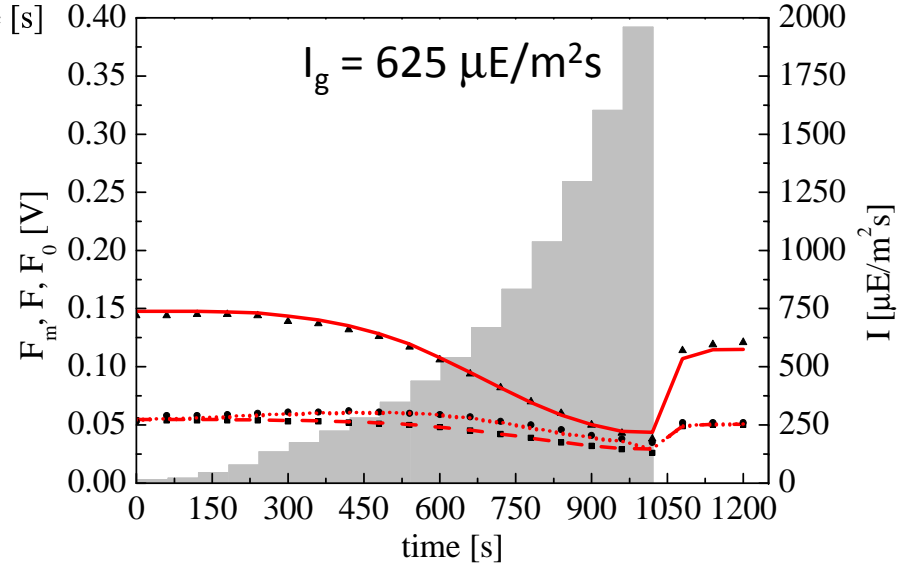
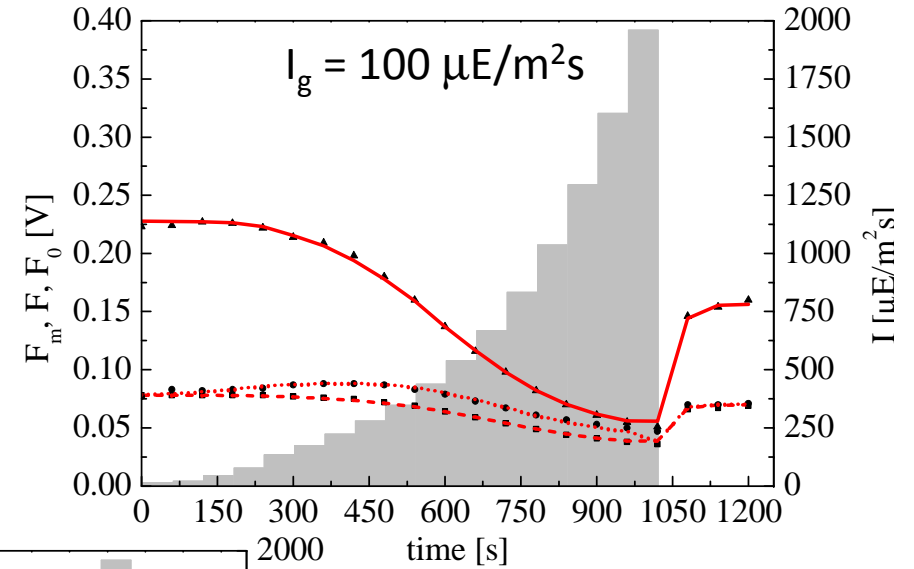
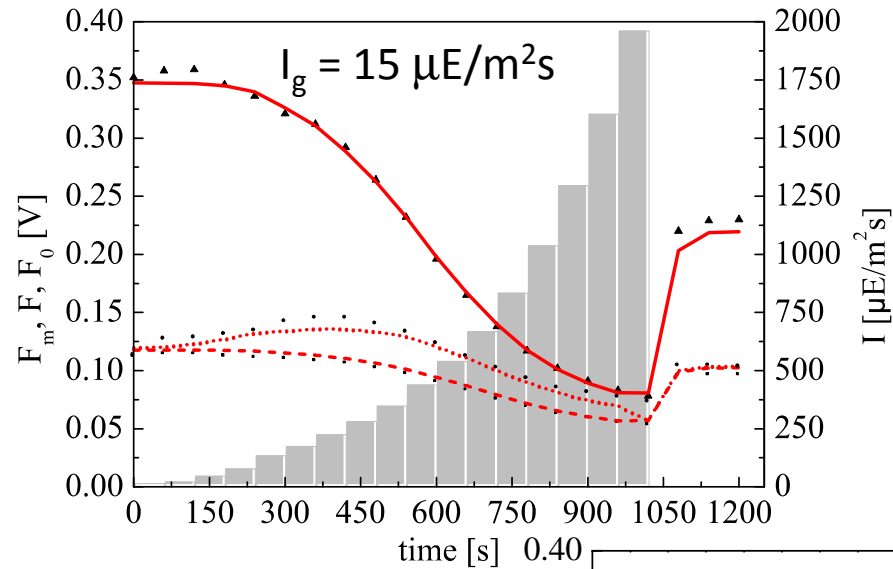
Photosynthetic process scheme (2)



Dynamic model of fluorescence

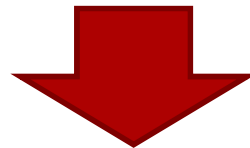


Model results



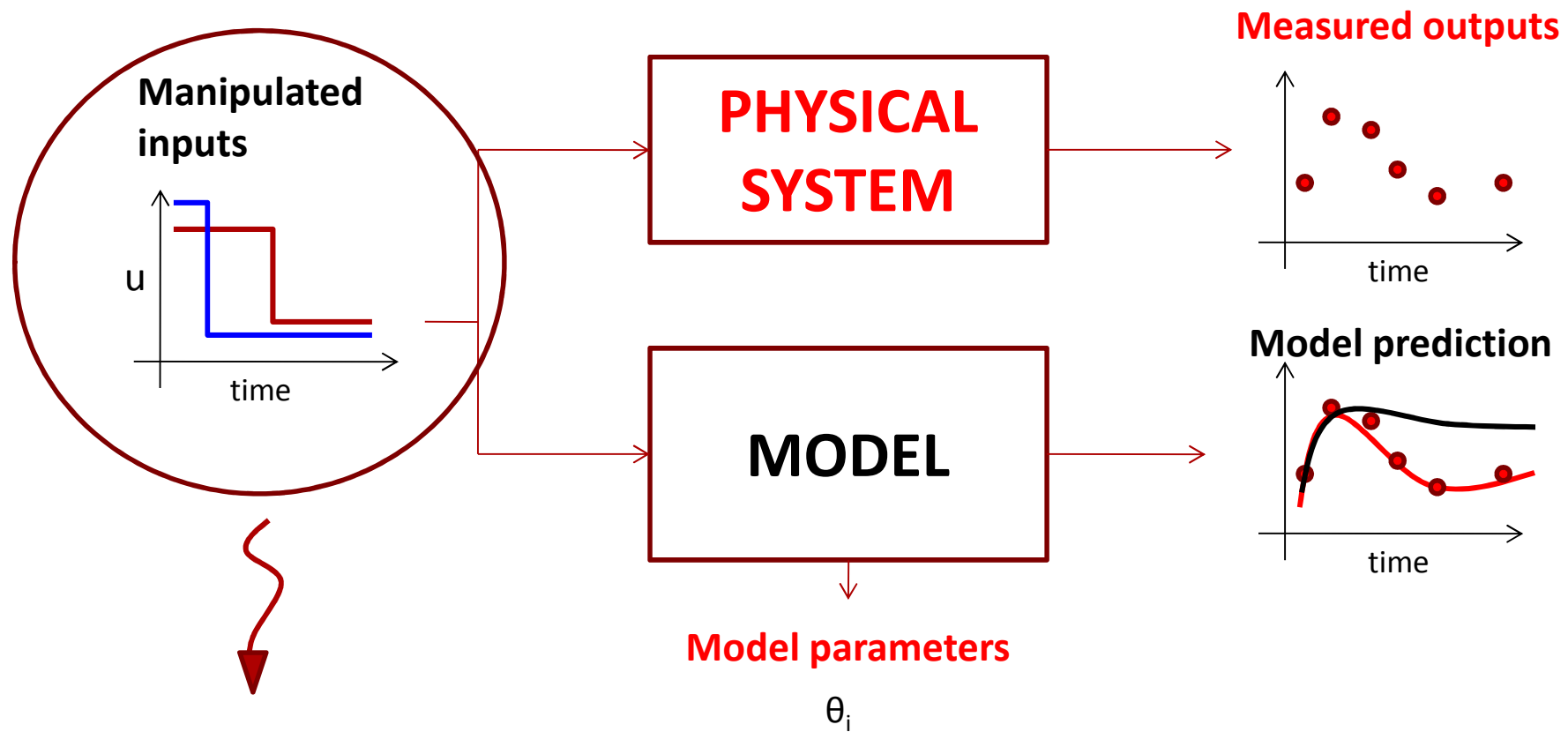
Issues

- Several issues at stake:
 - modelling hypotheses require experiments for discrimination and parametric validation
 - experiments are time consuming and costly and often blurred by:
 - intrinsic biological variability
 - limited number of measurements
 - concurrent phenomena happening at the same time (e.g. "interference" of biomass concentration and equipment design on light effects)



Propose more effective experimental devices coupled with advanced experimental design techniques

Model-Based Design of Experiments



Optimal input design

MBD_oE

Optimal design problem

$$\boldsymbol{\varphi}^{\text{opt}} = \arg \min_{\boldsymbol{\varphi}} \left\{ \Psi \left[\mathbf{V}_{\theta}(\boldsymbol{\theta}, \boldsymbol{\varphi}) \right] \right\} = \arg \min_{\boldsymbol{\varphi}} \left\{ \Psi \left[\mathbf{H}_{\theta}^{-1}(\boldsymbol{\theta}, \boldsymbol{\varphi}) \right] \right\} \quad \text{DESIGN OPTIMALITY}$$

subject to

$$f(\dot{\mathbf{x}}, \mathbf{x}, \mathbf{u}, \mathbf{w}, \boldsymbol{\theta}, t) = 0 \quad \hat{\mathbf{y}} = h(\mathbf{x}) \quad \text{DETERMINISTIC MODEL}$$

$$\tilde{\mathbf{C}} = z(\dot{\mathbf{x}}(t), \mathbf{x}(t), \dot{\mathbf{u}}(t), \mathbf{u}(t), \mathbf{w}, \boldsymbol{\theta}) \leq 0 \quad \text{FEASIBILITY CONDITIONS}$$

(Constraints on State Variables)

- $\mathbf{x}(t)$ n_s - dimensional vector of state variables
- $\mathbf{u}(t)$ n_u - dimensional vector of manipulated inputs
- \mathbf{w} n_w - dimensional vector of time-invariant inputs
- $\hat{\boldsymbol{\theta}}$ n_{θ} - dimensional vector of model parameters
- $\hat{\mathbf{y}}(t)$ M – dimensional vector of measured variables

Design vector

$$\boldsymbol{\varphi} = \left[\mathbf{y}(t_0), \mathbf{u}(t), \mathbf{w}, \mathbf{t}^{sp}, \boldsymbol{\tau} \right]$$

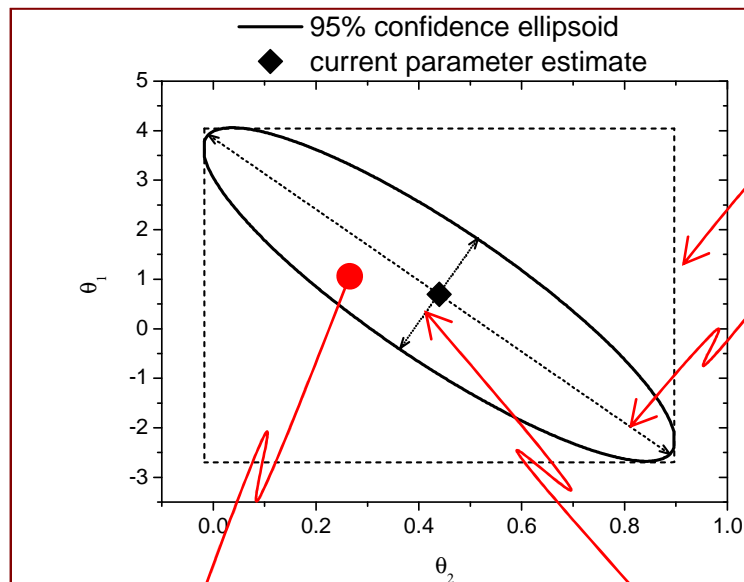
MBD_oE

DESIGN OPTIMALITY CONDITION

$$\boldsymbol{\varphi} = \arg \min_{\boldsymbol{\varphi}} \left\{ \left[\mathbf{V}_{\theta}(\boldsymbol{\theta}, \boldsymbol{\varphi}) \right] \right\} = \arg \min_{\boldsymbol{\varphi}} \left\{ \left[\mathbf{H}_{\theta}(\boldsymbol{\theta}, \boldsymbol{\varphi}) \right]^{-1} \right\}$$

Dynamic
Information
Matrix

Design Criteria



A-Optimal

E-Optimal

D-Optimal

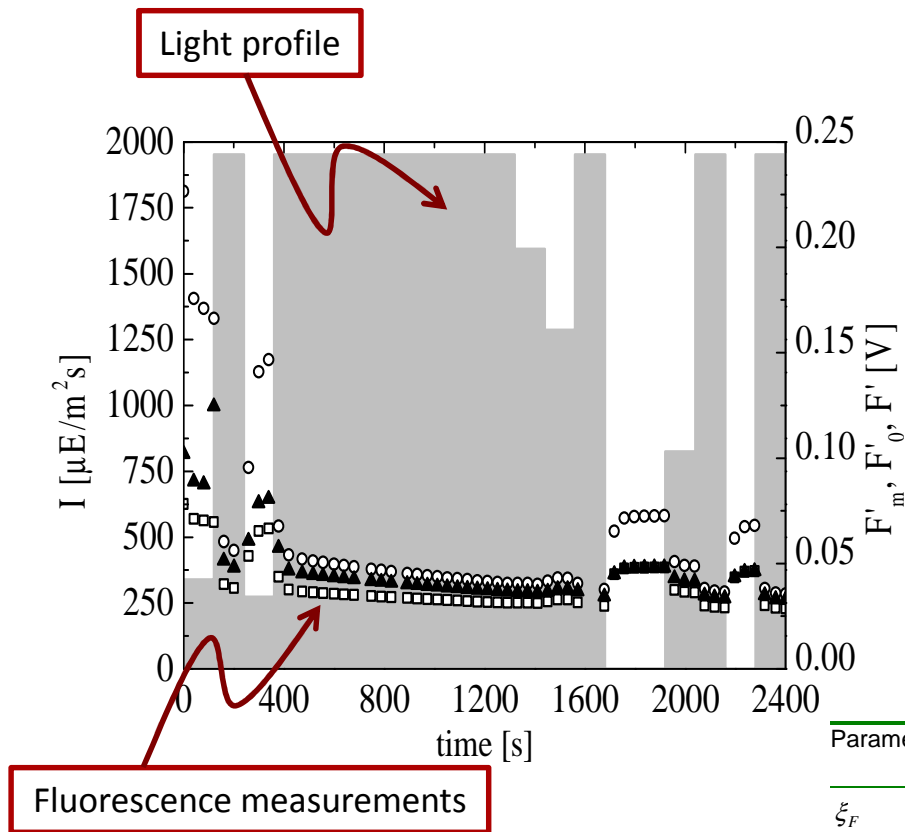
SV-Optimal

Preliminary
Information
Matrix

$$\mathbf{H}_{\theta}(\boldsymbol{\theta}, \boldsymbol{\varphi}) = \left[\sum_{k=1}^{n_{sp}} \sum_{i=1}^{N_y} \sum_{j=1}^{N_y} s_{ijk} \mathbf{Q}_{ik}^T \mathbf{Q}_{jk} + \mathbf{H}_{\theta}^0 \right]$$

Variance-covariance
of measurements
errors

Sensitivity
Matrix



Implementing MBDoe

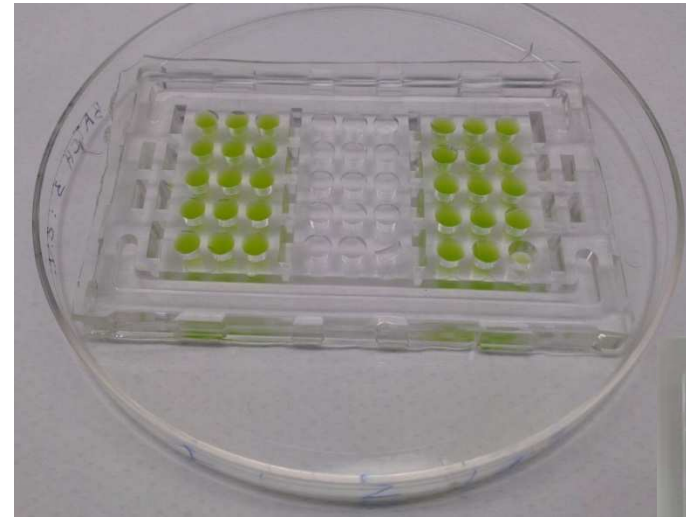
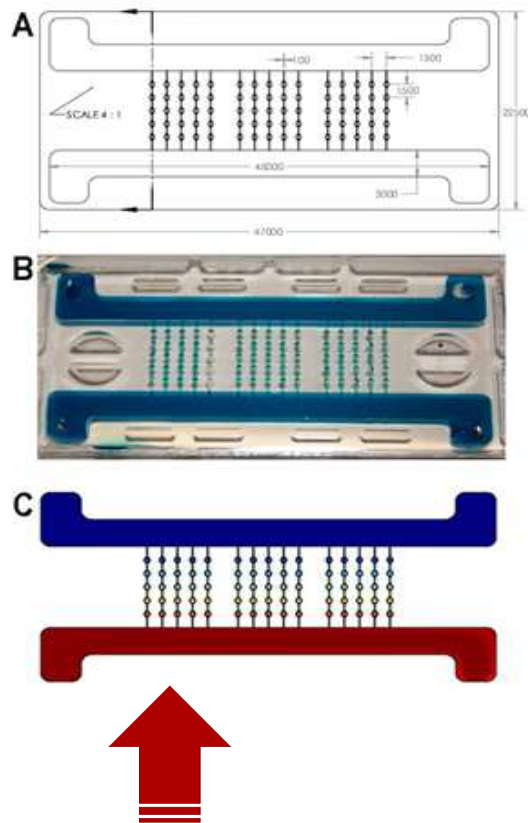
Demonstrated effectiveness of MBDoe
to **identify** model parameters

Standard experiment

Designed experiment

Parameter	Standard experiment			Designed experiment		
	Par. Value	95% Conf.Int.	t-val 95%	Par. Value	95% Conf.Int.	t-val 95%
	Non designed experiment			Optimally designed experiment		
ξ_F	$5.76 \cdot 10^{-2}$	$1.38 \cdot 10^{-2}$	4.07	$5.64 \cdot 10^{-2}$	$5.34 \cdot 10^{-3}$	10.82
I_{qE}	$8.13 \cdot 10^2$	$9.43 \cdot 10^1$	8.32	$9.49 \cdot 10^2$	$6.16 \cdot 10^1$	4.32
k_d	$7.06 \cdot 10^{-7}$	$1.76 \cdot 10^{-6}$	0.48*	$8.19 \cdot 10^{-7}$	$3.31 \cdot 10^{-7}$	2.18
n	$2.39 \cdot 10^0$	$2.31 \cdot 10^0$	10.71	$2.23 \cdot 10^0$	$1.74 \cdot 10^{-1}$	5.91
η_I	$7.84 \cdot 10^1$	$1.21 \cdot 10^2$	0.49*	$6.36 \cdot 10^1$	$3.29 \cdot 10^1$	2.53
$\bar{\eta}_{qE}$	$1.87 \cdot 10^1$	$1.79 \cdot 10^1$	7.89	$2.07 \cdot 10^1$	$1.16 \cdot 10^0$	6.84
η_p	$1.12 \cdot 10^1$	$3.12 \cdot 10^{-1}$	28.05	$1.15 \cdot 10^1$	$3.08 \cdot 10^{-1}$	16.55
S_f	$1.68 \cdot 10^0$	$2.82 \cdot 10^{-1}$	4.99	$1.55 \cdot 10^0$	$9.66 \cdot 10^{-2}$	6.07
σ	$8.13 \cdot 10^{-1}$	$1.52 \cdot 10^{-1}$	4.99	$8.82 \cdot 10^{-1}$	$1.85 \cdot 10^{-1}$	6.19

Prototyping the idea

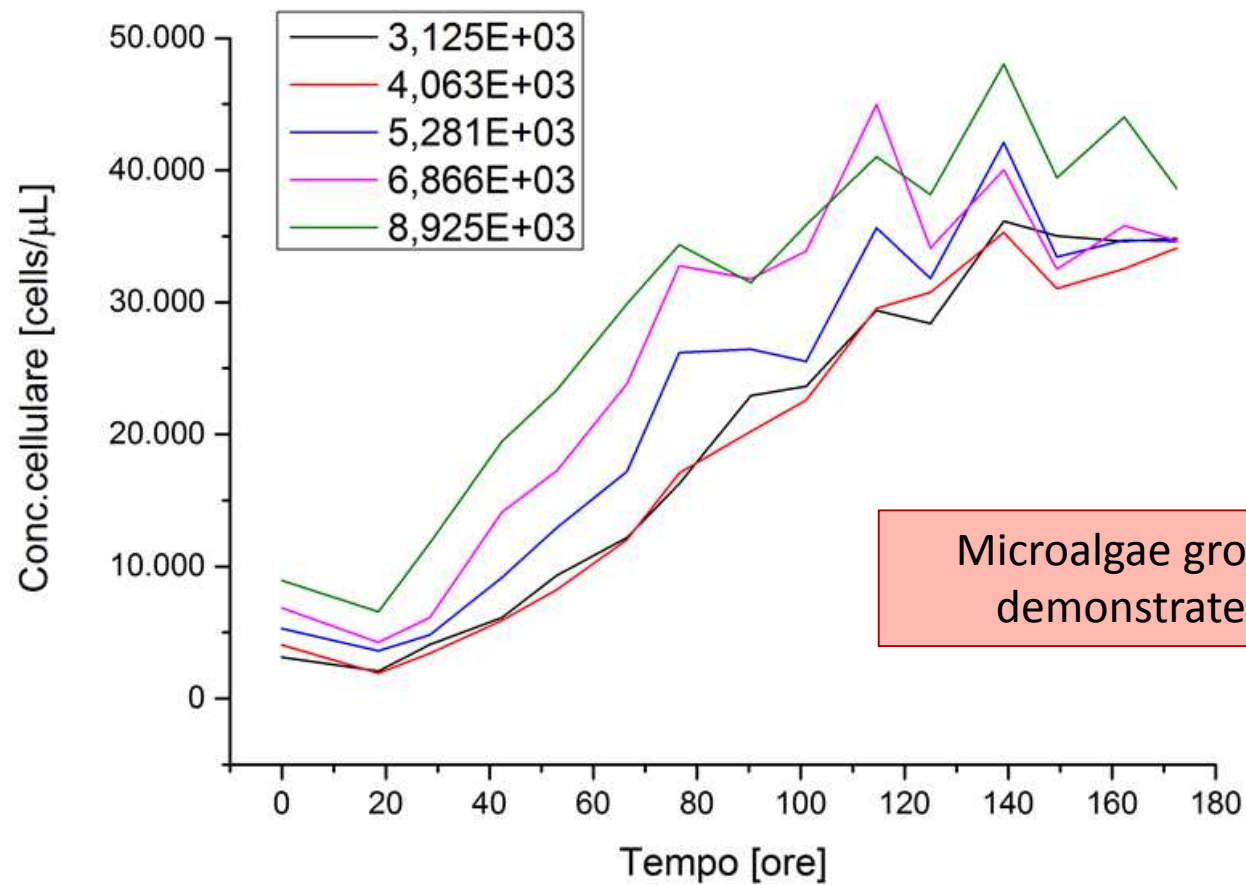


First prototype platforms already realised

Arrays of micro-photobioreactor on a microfluidic platform

- stable concentration gradients over a large number of cell samples
- possibility to generate multiple gradients of nutrients,
- possibility to apply fast dynamic changes of environmental signals (light)
- complex sequences of time- and space- resolved gradients
- continuous operation
- support of long-term culture of algae cells in a no-shear environment,
- high-throughput studies with large numbers of replicates
- compatibility with on-line imaging and standard analytics

Preliminary results



Future work

- Consolidate experimental and analytical techniques in microPBRs
- Move from batch to continuous operations
- Enhance model structure and validate it

Thank you for your attention