

# Competition and substitution in energy: old scenarios and emerging technologies

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## PhD in Statistical Sciences

1st year: courses for theoretical deepening of important mathematical and statistical topics

### Original project (started in October 2016)

- ✓ Dataset (Belgium, China, Finland, France, Germany, India, Japan, Spain, Sweden, Switzerland, UK, USA)
- Univariate diffusion models (unnecessary)
- ✓ UCRCO and CRCO models: 2 competitors
- Dynamic market potential (to be done in the next months)
- ✓ Incorporate intervention functions
- ✓ Extend the competition models: 3 competitors

## Competition among energy sources?

- Still, most of electricity produced with depleting energy sources (e.g., coal, gas, oil, nuclear).
- Beside the problem of fuel depletion, climate change and pollution produced by fossil fuels.
- Renewable sources of energy appear a viable option to deal with all these problem  
⇒ solar technology has already made significant progress in a short amount of time (The Economist, June 6, 2015).

Renewable energy sources is gaining market share against other sources.

## Two versions

### Balanced model

A model where the word-of-mouth (w.o.m) affects only at the category level instead of brand level, i.e. the w.o.m effect does not separate the adoptions of each brand from those of competitors.

### Unbalanced model

A model where the w.o.m affects at the brand level, i.e. separating the within-brand from the cross-brand w.o.m effects.

## Synchronic competition

It means there are simultaneous market entries for the competing brands (products).

## Diachronic competition

It means there are sequential market entries of the competing brands (products). Diachronic competition creates the 'regime change' problem for the previously entered pioneers.

Usually, feasible competition models deal with 2 products due to parameters' complexity

## Renewable

Renewable sources of energy are those that are replenished by the environment over relatively short periods of time. Solar, wind, water, biomass, etc.

## Non-renewable

Non-renewable energy comes from sources that will run out or will not be replenished in our lifetimes. Coal, gas, oil and nuclear.

**UCRCD model** (Guseo and Mortarino, 2012; 2014)

$$z_1'(t) = m \left[ \left( p_{1a} + q_{1a} \frac{z(t)}{m} \right) (1 - I_{t > c_2}) + \left( p_{1c} + (q_{1c} + \delta) \frac{z_1(t)}{m} + q_{1c} \frac{z_2(t)}{m} \right) I_{t > c_2} \right] \left( 1 - \frac{z(t)}{m} \right)$$

$$z_2'(t) = m \left( p_2 + (q_2 - \gamma) \frac{z_1(t)}{m} + q_2 \frac{z_2(t)}{m} \right) \left( 1 - \frac{z(t)}{m} \right) I_{t > c_2}$$

$$m = m_a (1 - I_{t > c_2}) + m_c I_{t > c_2}$$

$$z(t) = z_1(t) + z_2(t) I_{t > c_2}$$

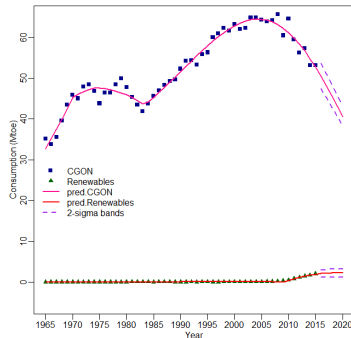
**Non-renewable (CGON):** coal, gas, oil, nuclear  
**Renewable** : hydro, solar, wind

CRCS model with 3 exp. shock for 2 competitors, Belgium

Parameter	Estimate	Standard Error	95% Confidence interval
m	3346.41	84.6301	(3178.22, 3514.59)
p1	0.07208	0.21886	(-0.36286, 0.50704)
q1	0.60419	1.79455	(-2.9621, 4.17049)
a1	5.97378	0.84601	(4.29251, 7.65504)
b1	-0.04530	0.02514	(-0.09528, 0.00466)
c1	0.12536	0.35290	(-0.57595, 0.826682)
a2	19.28340	0.51744	(18.25510, 20.31170)
b2	-0.00364	0.01091	(-0.02533, 0.01805)
c2	-0.99004	0.06914	(-1.12745, -0.85264)
p2	0.00025	0.01091	(-0.02143, 0.021947)
q2	0.01147	0.15821	(-0.30293, 0.32588)
a3	45.28640	3.61224	(38.10790, 52.46500)
b3	-0.05964	0.99596	(-2.03893, 1.91963)
c3	-0.98898	0.15527	(-1.29756, -0.680406)
$R^2=0.99855$ F test=7.42487			



**Non-renewable (CGON):** coal, gas, oil, nuclear  
**Renewable** : hydro, solar, wind



Fitted CRCS model with 3 exp. shocks (for confidence bands see, Guseo and Mortarino, 2015)

⇒ Not feasible for 7 products (coal, gas, oil, nuclear, hydro, solar, wind).

⇒ **Nuclear energy might be defined as renewable**  
(controversial in the literature)

- **CGO:** coal, gas, oil
- **Nuclear**
- **Renewable:** hydro, solar, wind

$$z'_1(t) = m \left\{ \left[ p_{1\alpha} + q_{1\alpha} \frac{z(t)}{m} \right] I_{t \leq c_2} + \left[ p_{1\beta} + q_{1\beta} \frac{z(t)}{m} \right] I_{c_2 < t \leq c_2} + \left[ p_{1\gamma} + q_{1\gamma} \frac{z(t)}{m} \right] I_{t > c_3} \right\} \left[ 1 - \frac{z(t)}{m} \right]$$

$$z'_2(t) = m \left\{ \left[ p_{2\beta} + q_{2\beta} \frac{z(t)}{m} \right] I_{c_2 < t \leq c_2} + \left[ p_{2\gamma} + q_{2\gamma} \frac{z(t)}{m} \right] I_{t > c_3} \right\} \times \left[ 1 - \frac{z(t)}{m} \right]$$

$$z'_3(t) = m \left[ \left( p_{3\gamma} + q_{3\gamma} \frac{z(t)}{m} \right) \right] \left[ 1 - \frac{z(t)}{m} \right] I_{t > c_3}$$

$$m = m_\alpha I_{t \leq c_2} + m_\beta I_{c_2 < t \leq c_3} + m_\gamma I_{t > c_3}$$

$$z(t) = z_1(t) + z_2(t) I_{t > c_2} + z_3(t) I_{t > c_3}$$

# Model fitted for 3 competitors



**CGO** : coal, gas, oil

**Nuclear**

**Renewable:** hydro, solar, wind

UCRCS model with 1 exp. shock for 3 competitors, Belgium

Parameter	Estimate	Standard Error	95% Confidence interval
m	3849.24	72.5341	(3705.82, 3992.65)
p1	0.00256	0.00103	(0.00052, 0.00460)
$\delta$	-0.23442	0.08316	(-0.39885, -0.07000)
$\eta$	0.25708	0.08544	(0.08814, 0.42603)
q1	0.2553	0.07444	(0.10810, 0.40250)
a1	8.86723	0.29263	(8.28864, 9.44581)
b1	-0.14734	0.02204	(-0.19092, -0.10376)
c1	2.32784	1.33721	(-0.31606, 4.97175)
p2	-0.00001	0.00016	(-0.00034, 0.00031)
$\theta$	0.00415	0.01184	(-0.01926, 0.0275731)
$\xi$	1.56074	0.44188	(0.68705, 2.43443)
q2	-0.00572	0.01063	(-0.02674, 0.01529)
p3	-0.00040	0.00016	(-0.00073, -0.00007)
q3	0.03467	0.01109	(0.01272, 0.05661)
$R^2=0.99550$		F test=43.20186	

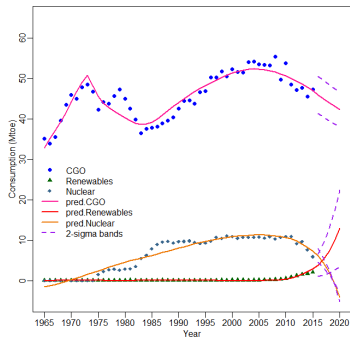
# 3 competitors



**CGO** : coal, gas, oil

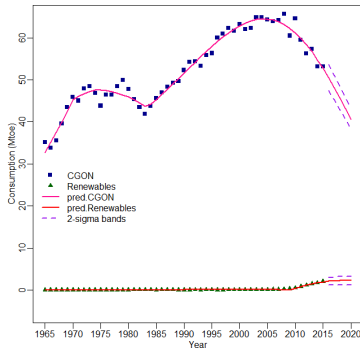
**Nuclear**

**Renewable**: hydro, solar, wind

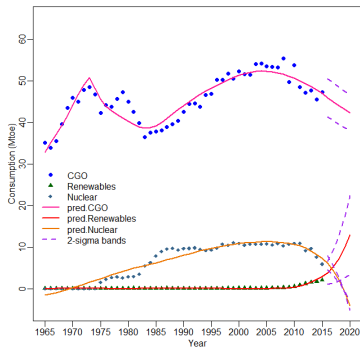


Fitted UCRCS model with 1 exp. shock; for confidence bands (see, Guseo and Mortarino, 2015)

**CGON:** coal, gas, oil, nuclear  
**Renewable:** hydro, solar, wind



**CGO:** coal, gas, oil  
**Nuclear**  
**Renewable:** hydro, solar, wind



- For almost all 12 countries analyzed our extended models for 3 competitors give narrower confidence bands than the existing models for 2 competitors.
- Narrower confidence bands correspond to a reduced forecasting uncertainty  
⇒ the new model allows more precise forecasting.

- Complete comparisons between 2-product models and 3-product models.
- Improve model accuracy with a more flexible market potential definition (in the analyzed models a fixed market potential was assumed).
- Evaluate feasibility of 4-product models



- 1** Guseo, R. and Mortarino, C. (2012). Sequential market entries and competition modeling in multi-innovation diffusions. *European Journal of Operation Research* 216:658-667.
- 2** Guseo, R. and Mortarino, C. (2014). Within-brand and cross-brand word-of-mouth for sequential multi-innovation diffusions. *IMA Journal of Management Mathematics* 25:287-311.
- 3** Guseo, R. and Mortarino, C. (2015). Modeling competition between two pharmaceutical drugs using innovation diffusion model. *The Annals of Applied Statistics* 9(4):2073-2089.
- 4** Savin, S. and Terwiesch, C. (2005). Optimal product launch times in a duopoly: balancing life-cycle revenues with product cost. *Operation Research* 53:26-47.

**Thank you for your kind  
attention!**

